

## 7.6 Notes

Tuesday, May 12, 20

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## Section 7.6 – Vertex Form

### o Vertex Form

$$y = a(x - h)^2 + k$$

- Vertex:  $(h, k)$
- Axis of Symmetry:  $x = h$
- Parabola opens up when  $a > 0$ . The minimum value of the
- Parabola down up when  $a < 0$ . The maximum value of the
- Can tell you if there are one, two, or no zeros.
  - o Two Zeros: the graph has a positive value or 0 for  $k$  value for  $k$ .
  - o One Zero: the graph has no value for  $k$  and  $h$  is 0.
  - o No Zeros: the graph has a negative value for  $h$  and  $k$ .
- Benefits: you sketch a graph more easily from this form.
- Drawbacks: looks outlandishly hard. (But it isn't, so this doesn't act

### 7.6 Examples

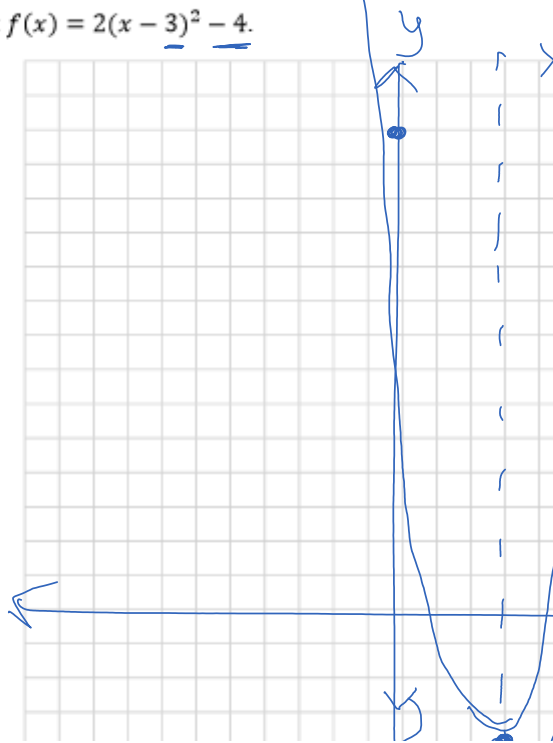
1. Sketch the following function:  $f(x) = 2(x - 3)^2 - 4$ .

$$\text{Vertex: } (3, -4)$$

$$\begin{aligned} f(0) &= 2(0-3)^2 - 4 \\ &= 2(-3)^2 - 4 \\ &= 18 - 4 \\ &= 14 \end{aligned}$$

$$(0, 14)$$

$$\text{AoS} \Rightarrow x = 3$$



## 7.6 Continued

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3. A soccer ball is kicked from the ground. After 2 seconds, the ball reaches its maximum height of 20 m. It lands on the ground after 4 seconds.

a. Determine the quadratic function that models the height of the kick.

$$y = a(x-h)^2 + k$$

$$h = a(x-t)^2 + h \rightarrow \text{y-intercept } t / \text{"c value"}$$

$$h = a(x-2)^2 + 20$$

$$0 = a(4-2)^2 + 20$$

$$0 = a(4) + 20$$

$$-20 = 4a$$

$$h = -5(x-2)^2 + 20$$

b. Determine any restrictions on the domain and range for this problem.

$$\{t \mid t \geq 0, t \in \mathbb{R}\}$$

$$\{h \mid h \geq 0, h \in \mathbb{R}\}$$

c. What was the height of the ball at 1 second?

$$h = -5(1-2)^2 + 20$$

$$h = -5(-1)^2 + 20$$

$$h = -5(1) + 20$$

$$h = -5 + 20$$

$$h = 15$$

\* The height of the ball is 15 m.

d. When is the ball at the same height on the way down?

Option 1: solve for x (factoring + stuff)

Option 2: Line of sym (aka the axis of symmetry)

$$x = 2 \quad \infty \quad L \cup S \quad (\text{vertex is at } (2, 20))$$

$$(1, 15)$$

$$2-1=1$$

$$(3, 15)$$

↑

↑

1 sec

15 m

$$2+1=3$$

on the way down